

EFFECT OF AUSTENITE GRAIN MORPHOLOGY ON VARIANT SELECTION OF MARTENSITE TRANSFORMED FROM ULTRAFINE-GRAINED AUSTENITE

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Abstract: In this research, variant selection of martensite transformed from ultrafine-grained (UFG) austenite fabricated by accumulative roll bonding (ARB) process and subsequent annealing was investigated with respect to morphology of parent austenitic phase. The results show that the original shape of austenite grain is very effective factor in determining the preferred variants of martensite transformed from the elongated ultrafine-grained austenite fabricated by 6-cycles via the ARB process. Annealing treatment of the austenitic samples subjected to the 6-cycle ARB processed at 873 K for 1.8 ks suppressed the variant selection by changing the morphology of austenite grains from elongated ultrafine-grains to fully-recrystallized and equiaxed fine-grains.

Keywords: Martensitic transformation, Accumulative roll bonding, Ultrafine-grained austenite, Variant selection, Severe plastic deformation.

1. INTRODUCTION

In recent years, bulky ultrafine grained (UFG) materials fabricated by severe plastic deformation with a mean grain size of less than 1 μm have been comprehensively studied, due to their superior mechanical properties [1-5]. A significant large area of grain boundaries per unit volume in UFG materials can affect martensitic transformation behavior as habit plates within martensitic structures cannot grow beyond grain boundaries. Previous studies clearly indicated that martensitic transformation can be significantly influenced by austenite grain size [6-11]. Umemoto and Owen [6] demonstrated that martensite transformation starting temperature (M_s) decreases with decrease of the austenite grain size. Maki et al. [7] studied the variety of martensite morphologies produced after being transformed from various grain sizes of austenite at different temperatures. Their results indicated that the refinement of austenite grains decreases the M_s , resulting to a change in martensite morphology. Although several studies have been reported on the austenite grain-

size effects [8-11], but there is no deep systematic study of the martensitic transformation from ultrafine-grained austenite.

It is well known that martensite usually satisfies Kurdjumov-Sachs (K-S) orientation relationship with respect to austenite ($\{111\}_A // \{011\}_M, <101>_A // <111>_M$, where subscripts A and M represent austenite and martensite, respectively) [12]. When the K-S relationship is maintained, 24 equivalent crystallographic variants of martensite can form from a single crystal of austenite. Table 1 summarizes the orientation relationships between the 24 crystallographic variants (V_1 - V_{24}) of martensite and austenite under K-S orientation relationship.

When plastic deformation is introduced to austenite before martensitic transformation, the 24 variants of martensite do not form equally and some specific variants are preferentially formed, resulting to formation of transformation texture. This is so-called variant selection. Recently Chiba et al. [13] reported that variants of lenticular martensite habit planes that were closely parallel to compression planes which were favorably formed during ausforming of

Table 1. The 24 crystallographic variants of martensite for the K-S orientation relationship

Variant	Plane parallel	Direction parallel
V ₁	(111) _A //(011) _M	$[\bar{1}01]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₂		$[\bar{1}01]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₃		$[01\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₄		$[01\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₅		$[1\bar{1}0]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₆		$[1\bar{1}0]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₇	($\bar{1}\bar{1}\bar{1}$) _A //(011) _M	$[0\bar{1}1]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₈		$[0\bar{1}1]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₉		$[\bar{1}0\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₀		$[\bar{1}0\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₁		$[110]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₂		$[110]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₃	($1\bar{1}\bar{1}$) _A //(011) _M	$[10\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₄		$[10\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₅		$[\bar{1}\bar{1}0]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₆		$[\bar{1}\bar{1}0]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₇		$[011]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₈		$[011]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₁₉	($1\bar{1}\bar{1}$) _A //(011) _M	$[\bar{1}\bar{1}0]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₂₀		$[\bar{1}\bar{1}0]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₂₁		$[0\bar{1}\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₂₂		$[0\bar{1}\bar{1}]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₂₃		$[101]_A // [\bar{1}\bar{1}\bar{1}]_M$
V ₂₄		$[101]_A // [\bar{1}\bar{1}\bar{1}]_M$

austenite. Lef et al. [14] investigated variant selection of mechanically induced martensite transformed from metastable austenite. They found that interaction energy between externally applied stress and lattice deformation can determine preferential martensite variants based on Patel and Cohen's theory [15]. Recently, the present authors demonstrated that variant selection rule can be changed in severely deformed UFG austenite depending on amount of induced strain [16]. However, variant selection of martensite in UFG austenite has been rarely studied. So the aim of this study is to clarify the variant selection rules of martensite transformed from ultrafine-grained austenite with respect to

morphology of austenite grains, i.e., austenite grain size and shape.

2. MATERIALS AND METHODS

An Fe-24Ni-0.3C (wt.%) alloy, of which chemical composition is shown in Table 2, was used in the present study. A cast ingot of the alloy was hot-rolled and then cold-rolled to make sheets with thickness of 1 mm. The sheets were austenitized at 1173 K for 3.6 ks for obtaining a fully recrystallized and coarse-grained austenite with a mean grain size of 35 μm. To obtain ultrafine-grained austenite structures, the austenitized sheets were subjected to

Table 2. Chemical composition of the alloy studied (wt.%)

Fe	C	Ni	Si	Mn	P	S	O	N
bal.	0.29	24.09	0.01	0.07	<0.005	<0.0005	0.0008	0.0006

accumulative roll bonding (ARB) process. Figure 1 is a schematic illustration showing the principle of the ARB process [3]. In the ARB process, two pieces of the sheets 1 mm thick are stacked after degreasing and wire brushing the contact surfaces. The stacked sheets are roll-bonded by 50% reduction in one pass. Then, the roll-bonded sheet is cut into two, stacked to have the initial dimensions before rolling, and the procedures described above are repeated again. The ARB process can apply significant amount of plastic strain into materials, because the procedures can be repeated limitlessly. In order to prevent deformation-induced martensitic transformation during the present ARB process for obtaining fully austenitic structures, stacked sheets were held at 873 K, at which austenite phase of the studied alloy is stable, for 0.6 ks and subsequently roll-bonded. The roll-bonded sheets were immediately cooled in water. The roll-bonding was carried out under lubrication condition by the use of a two-high mill having a roll diameter of 310 mm. The ARB was repeated up to 6-cycle, so that total equivalent strain accumulated was 4.8. The 6-

cycle ARB processed specimens were annealed at 773, 823 and 873 K for 1.8 ks to obtain UFG austenite with partly recrystallized or fully recrystallized microstructures. The specimens subjected to the above mentioned treatments were cooled down to 77 K (in liq. N₂) to obtain thermally induced martensite.

The microstructures of the specimens before and after martensitic transformation were characterized by electron backscatter diffraction (EBSD) in a scanning electron microscope (SEM) equipped with a field-emission electron gun (Philips XL30S-FEG) operated at 15 kV. EBSD measurements were carried out with step size of 0.05 μm which were smaller than the interval of austenite grain boundaries. The sections of the specimen for EBSD observation were polished mechanically and then electrolytically in a 900mL CH₃COOH+100mL HClO₄ solution at approximately 284K with a voltage of 20V. The obtained EBSD data were analyzed by TSL-OIM Analysis software Ver. 6.1.3.

3. RESULTS AND DISCUSSION

3. 1. Microstructure of Austenite

In Fig. 2, microstructure of austenite processed by ARB is illustrated by grain boundary and phase maps obtained by EBSD measurements and analysis. In the grain boundary maps, high angle boundaries with misorientation larger than 15° are drawn in black lines and low angle boundaries with misorientation between 2° and 15° are drawn in red lines. In addition, martensite and austenite phases are shown in pink and green colors, respectively. The grain boundary map of Fig. 2(a) indicates that the starting material consists of fully recrystallized and coarse grained austenite. The phase maps of Fig. 2(a)-(e) demonstrate 100% austenite structures, indicating that deformation-induced martensitic transformations did not occur during

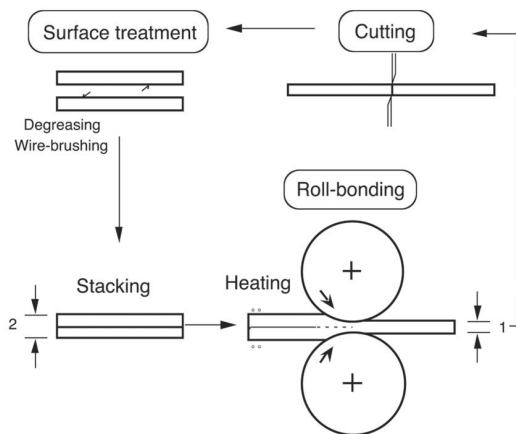


Fig. 1. Schematic illustration showing the principle of the accumulative roll bonding (ARB) [22].

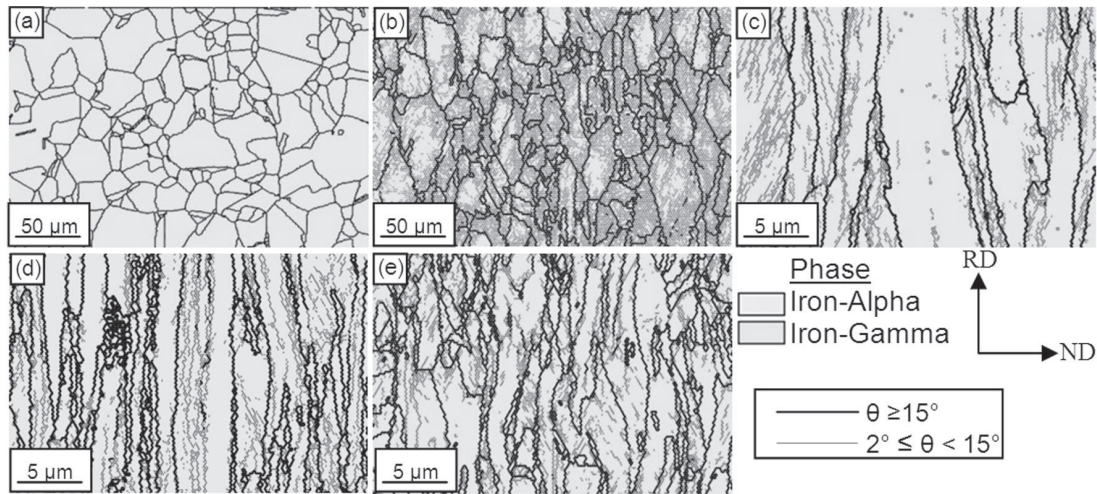


Fig. 2. (a)-(e) Grain boundary and phase maps of the starting material, 1-cycle, 2-cycle, 4-cycle and 6-cycle ARB processed specimens, respectively.

the ARB process at 873 K. The 1-cycle ARB process, corresponding to 50% rolling or an equivalent strain of 0.8, introduced a large amount of low angle boundaries into the austenite. Till 2-cycle of ARB process (75% rolling), the microstructures exhibit typical deformation microstructures which mainly involve pancake shape austenite grains having low angle boundaries (dislocation structures) inside. Increasing the number of ARB process up to 6-cycle causes significant grain refinement as shown in Fig. 2(e).

The grain boundary and phase maps of austenite ARB processed by 6-cycle and subsequently annealed at 773, 823 or 873 K for 1.8 ks are shown in Fig. 3. The grain boundary map of the specimen annealed at 773K (Fig. 3(a)) shows that the microstructure still consists of UFG lamellar structure, indicating that annealing at 773 K does not cause recrystallization of austenite. Grain boundary map of Fig. 3(b) indicates that recrystallization occurs partly by increasing the annealing temperature to 823 K. The recrystallized regions are free of low angle boundaries. Annealing treatment at 873 K results in fully recrystallized and equiaxed austenite with mean grain size of 2.5 μm, as shown in Fig. 3(c). Moreover, phase maps superimposed on grain boundary maps show that no phase transformation occurs during annealing treatments.

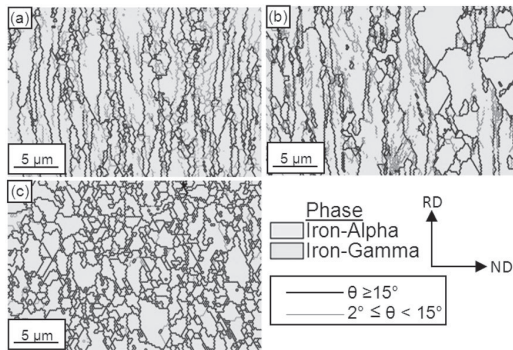


Fig. 3. (a)-(c) Grain boundary and phase maps of the specimens ARB processed by 6-cycle and annealed at 773, 823 and 873 K respectively.

Change in austenite grain size with increasing the number of ARB cycle and subsequent annealing is summarized in Fig. 4. Interception method was used to measure the grain size (or interval of boundaries) along normal direction (ND). Here, high angle boundaries were taken into account for the grain size (d_{HAGB}) measurement. The figure indicates that the grain size monotonously decrease with increasing strain (ARB cycle), and UFG austenite with mean grain size of 750 nm was obtained by 6-

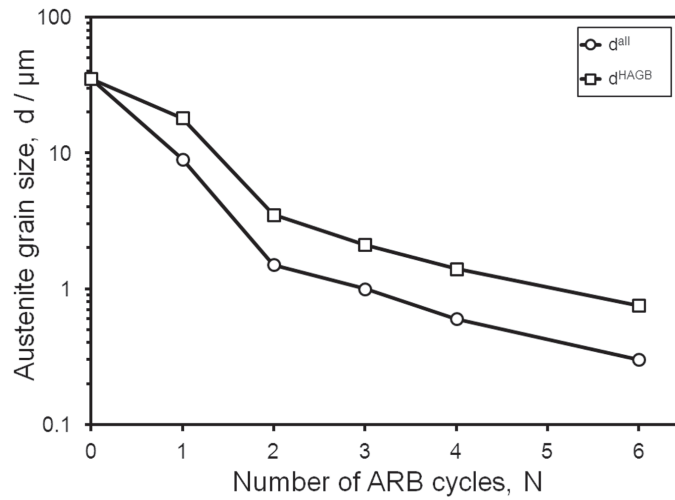


Fig. 4. Change in austenite grain size (boundary interval along ND) with the number of the ARB cycles and subsequent annealing.

cycle ARB process. Annealing treatment of austenite ARB processed by 6-cycle result in increasing of austenite grain size up to 2.5 μm at annealing temperature of 873 K as shown in Fig. 4.

3. 2. Variant Selection of Martensite

Figure 5(a) and (b) show an EBSD orientation map and corresponding $\{100\}_A$ pole figure of the

starting material. The colors in the orientation map indicates the crystallographic directions of each point parallel to TD of the sheet (the normal direction of the observed plane), according to the stereographic triangle shown in the figure. The ideal $\langle 100 \rangle_A$ axes of typical texture components in f.c.c crystal, i.e., Brass component ($\{110\}\langle 112 \rangle_A$), Copper component ($\{112\}\langle 111 \rangle_A$), S component ($\{123\}\langle 634 \rangle_A$),

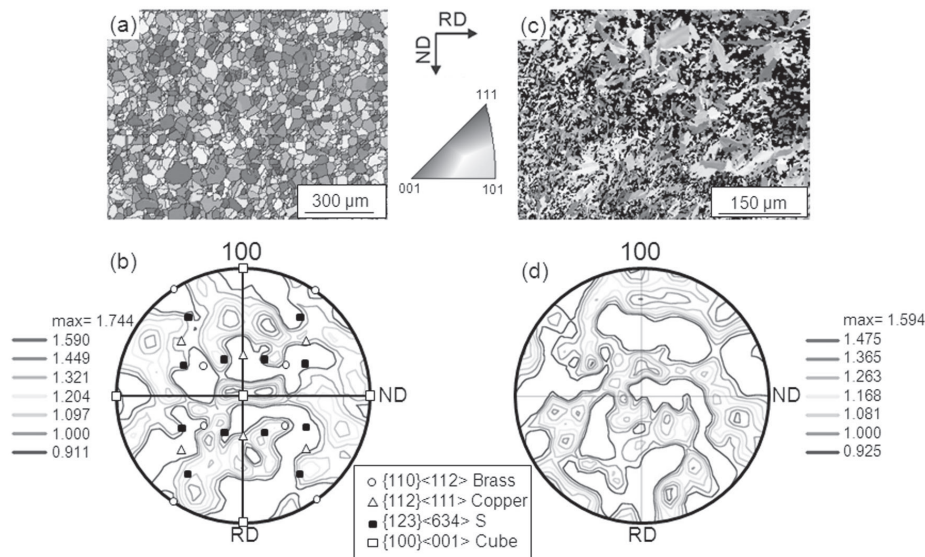


Fig. 5. ((a), (b)) EBSD orientation color map and $\{100\}$ pole figure of austenite before martensitic transformation in the starting material. ((c), (d)) EBSD orientation color map and $\{100\}$ pole figure of martensite after martensitic transformation in the starting material.

and Cube component ($\{100\}\langle 001\rangle_A$) are also indicated in the $\{100\}_A$ pole figure as circles, triangles, solid rectangles and open rectangles, respectively. The austenite of the starting material consists of equiaxed grains with a mean grain size of $35\ \mu\text{m}$, and does not have a particular texture, as shown in Fig. 5(a) and (b). An EBSD orientation map and corresponding $\{100\}_M$ pole figure of martensite in the starting material after thermally-induced martensitic transformation are shown in Fig. 5(c) and (d). Because the intensities in the pole figure of Fig. 5(d) are very weak (max. value is 1.594), it can be said that transformation texture is not developed during thermal martensitic transformation from the starting material having coarse-grained austenite with random texture.

The EBSD orientation map and corresponding $\{100\}_A$ pole figure of austenite after 6 cycles of ARB are shown in Fig. 6(a) and (b). Figure 6(c) and (d) displays the EBSD orientation maps and corresponding $\{100\}_M$ pole figures of martensite transformed from the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite. The colors in the orientation maps again indicate the crystallographic directions of

each point parallel to TD of the sheets. Preferentially formed variants of martensite can be determined by comparing the experimentally measured $\{100\}_M$ pole figure with the stereographic projection on which $\langle 100\rangle_M$ axes of the ideal 24 variants of martensite are plotted. The positions of the ideal $\langle 100\rangle_M$ axes for the 24 variants of martensite transformed from the austenite with exact Brass orientation ($(011)[2\bar{1}1]_A$) are plotted in Fig. 6(d). It reveals that the $V_6, V_{16}, V_{19}, V_{21}, V_{22}$ and V_{24} are preferentially formed during martensitic transformation from the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite.

Kundu [17] demonstrated that variant selection in thermally-induced martensitic transformation from cold-rolled austenite can be predicted from interaction energy between residual stress in the cold-rolled austenite and shape deformation accompanying martensitic transformation. However, the authors clearly demonstrated that the variant selection in martensitic transformation from the ultrafine-grained austenite fabricated by the 6-cycle ARB process is not determined by the interaction energy between the residual stress inherited by ARB

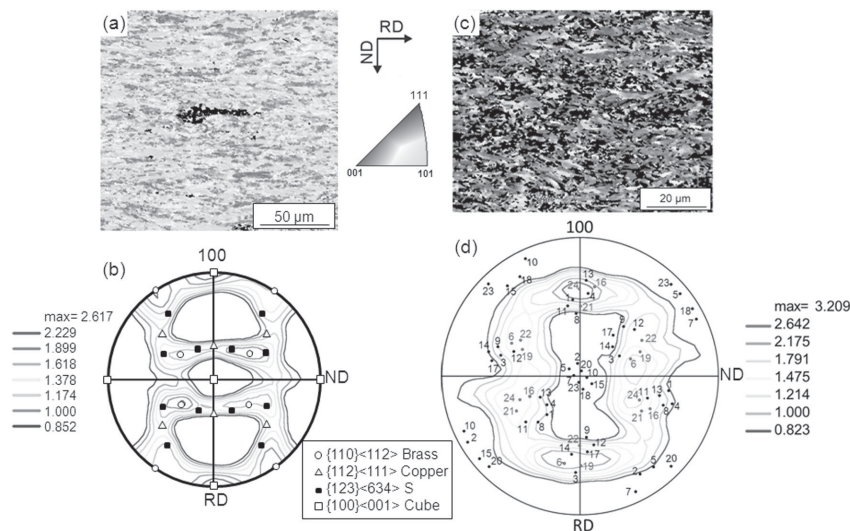


Fig. 6. EBSD orientation color maps and $\{100\}_A$ pole figures of austenite after 6 cycles of ARB process ((a), (b)) EBSD orientation color maps and $\{100\}_M$ pole figures of martensite transformed from the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite ((c), (d)). The positions of the ideal $\langle 100\rangle_M$ axes for the 24 variants of martensite transformed from the austenite with exact Brass orientation ($(011)[2\bar{1}1]_A$) from the austenite are shown by the numbers in $\{100\}_M$ pole figure of (d). The preferential variants are indicated by red color.

process and shape deformation [16].

As explained, the austenite after 6-cycle of ARB exhibits lamellar structure elongated along the rolling direction (RD) of the sheet. The average interval of high angle boundaries along the ND of the sheet is about 750 nm. This is a typical ultrafine grained structure fabricated by the ARB process. Since martensite plate cannot grow across high angle boundaries of austenite, it seems that the lamellar shape (elongated along RD) of the ultrafine-grained austenite (Fig. 2(c)) affects the variant selection of martensite transformed from the 6-cycle ARB processed specimen. On this basis, habit plane orientations for the 24 variants of martensite are plotted on the pole figure of which coordinate system corresponds to Brass orientation (RD // $[2 \bar{1} 1]_A$, ND // $[011]_A$), as shown in Fig. 7. The pole figure of Fig. 7 reveals that the normal directions of habit planes for the preferentially formed variants of martensite transformed from the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite (represented by red color) are nearly parallel to ND (V_6, V_{16}) or TD ($V_{19}, V_{21}, V_{22}, V_{24}$). The martensite plates of which normal directions of habit planes are parallel to ND or TD can grow along the elongated direction of the

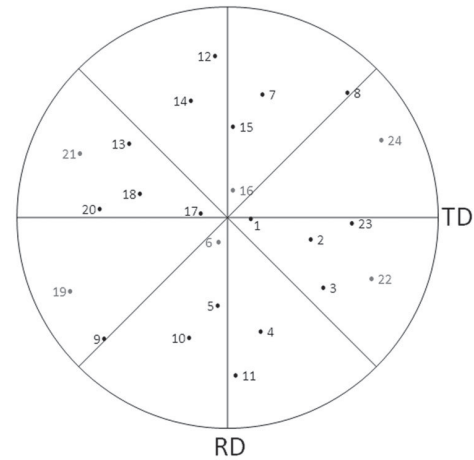


Fig. 7. A pole figure showing the habit plane orientation for the 24 variants of martensite. The preferentially formed variants of martensite transformed from the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite are indicated by red color. The coordinate system of the pole figure corresponds to the Brass texture (RD = $[2 \bar{1} 1]_A$, ND = $[011]_A$), which was found in the 6-cycle ARB processed austenite. The numbers indicate the positions of the habit plane orientation for the 24 variants of martensite transformed from the austenite with exact Brass orientation ($(011) [2 \bar{1} 1]_A$).

ultrafine-grained austenite in the 6-cycle ARB processed specimen. Therefore, it can be

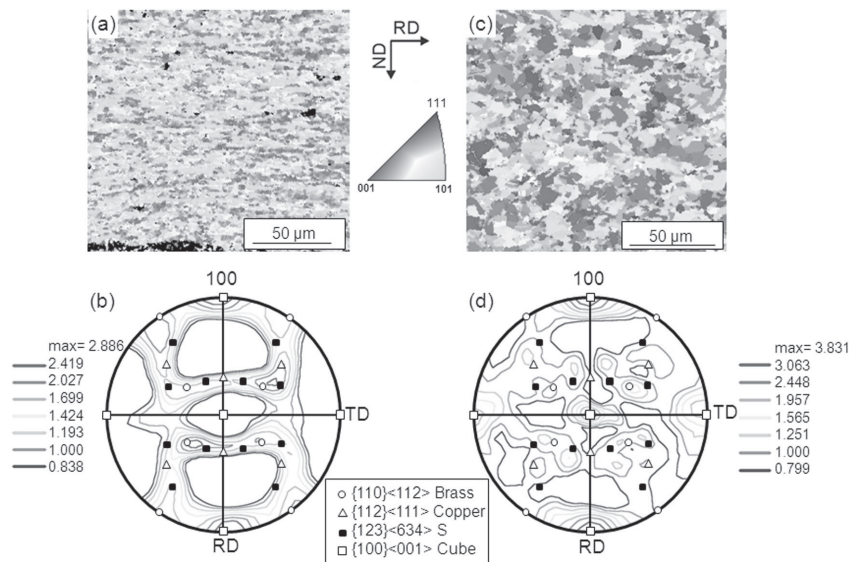


Fig. 8. EBSD orientation color maps and $\{100\}_A$ pole figures of austenite in ((a), (b)) the specimen 6-cycle ARB processed and then annealed at 773 K for 1.8 ks, and ((c), (d)) the specimen 6-cycle ARB processed and then annealed at 873 K for 1.8 ks.

concluded that in the case of the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite, austenite grain shape significantly affects the variant selection in martensitic transformation.

Figure 8(a) and (b) shows an EBSD orientation map and corresponding $\{100\}_A$ pole figure of the 6-cycle ARB processed specimen after annealing at 773 K for 1.8 ks. The 6-cycle ARB processed specimen still consists of elongated ultrafine-grained austenite after annealing at 773 K. In addition, Brass texture is kept after annealing at 773 K. This is because annealing at 773 K causes no recrystallization but only recovery, as explained. In contrast, recrystallization occurs by annealing at 873 K for 1.8 ks, resulting in the development of Cube texture as shown in Fig. 8(c) and (d).

Figure 9 (a) and (b) displays the EBSD orientation map and corresponding $\{100\}_M$ pole figure of martensite transformed from the austenite 6-cycle ARB processed and then annealed at 773 K for 1.8 ks having elongated ultrafine-grains. The positions of the ideal $\langle 100 \rangle_M$ axes for the 24 variants of martensite

transformed from the austenite with exact Brass orientation ($(011) [2 \bar{1} 1]_A$) are plotted in Fig. 9(b). The preferentially formed variants of martensite transformed from the 6-cycle ARB processed specimen after annealing at 773 K are $V_6, V_{16}, V_{19}, V_{21}, V_{22}$ and V_{24} , which are completely the same as those transformed from the 6-cycle ARB processed specimen (Fig. 6(d)). This fact supports the previous conclusion that the variant selection rule is determined by austenite grain shape, and not by interaction energy between the residual stress of austenite and shape deformation, when the austenite has elongated ultrafine-grained structures because the residual stress of austenite, which is inherited during the 6-cycle ARB process, is released to some extent by annealing at 773 K.

Figure 9(c) and (d) show an EBSD orientation map and corresponding $\{100\}_M$ pole figure of martensite transformed from the austenite 6-cycle ARB processed and then annealed at 873 K for 1.8 ks having equiaxed (recrystallized) fine-grains. Although the austenite 6-cycle ARB processed and then annealed at 873 K for 1.8 ks has the strong cube texture (Fig. 8(c)), the

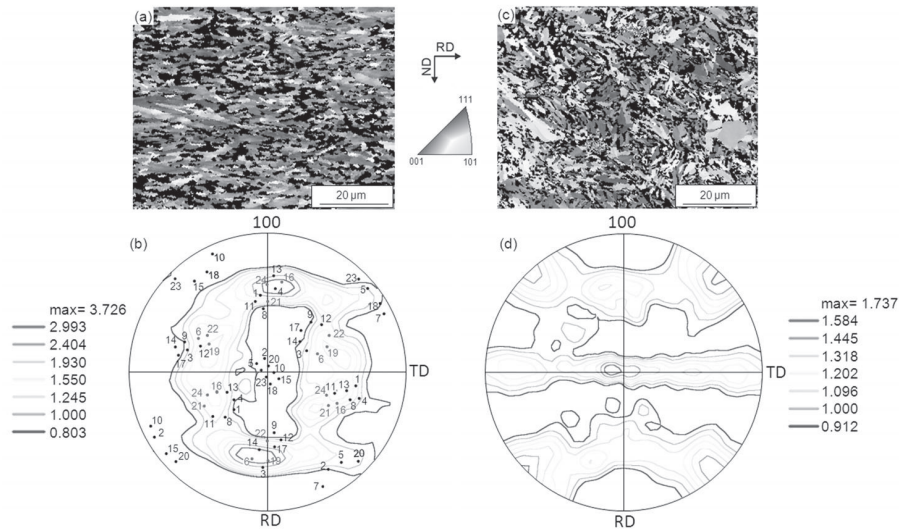


Fig. 9. EBSD orientation color maps and $\{100\}_M$ pole figures of martensite transformed from ((a), (b))the specimen 6-cycle ARB processed and then annealed at 773 K for 1.8 ks, and ((c), (d)) the specimen 6-cycle ARB processed and then annealed at 873 K for 1.8 ks. The positions of the ideal $\langle 100 \rangle_M$ axes for the 24 variants of martensite transformed from the austenite with exact Brass orientation ($(011) [2 \bar{1} 1]_A$) are shown in by the numbers (b). The preferential variants are indicated by red color.

intensities of martensite in the pole figure of Fig. 9(d) are very weak. This indicates that there is no variant selection of martensite transformed from the austenite having fully recrystallized and equiaxed grains even when austenite grain size is very fine.

4. CONCLUSIONS

In this paper, effect of austenite grain morphology on variant selection of martensite transformed from the ARB processed specimens having elongated ultrafine-grained austenite (the 6-cycle ARB processed specimen) and equiaxed fine-grained austenite (the specimen 6-cycle ARB processed and annealed at 873 K for 1.8 ks), was studied in the Fe-24Ni-0.3C alloy. The conclusions are summarized as follows:

1. The ARB process resulted in ultra-grain refinement of austenite. The obtained ultrafine grained (UFG) austenite consisted of the lamellar grains elongated along the rolling direction (RD) with mean grain thickness of 750 nm after 6-cycle of the ARB process. The starting material had random texture, while the 6-cycle ARB processed austenite exhibited the development of strong Brass component.
2. The variant selection in martensitic transformation from the 6-cycle ARB processed specimen having elongated ultrafine-grained austenite indicated that the elongated grain shape played an important role for the variant selection of martensite, i.e., the martensite plates which can grow along the elongated direction of the ultrafine-grained austenite were preferentially formed.
3. Annealing treatment of the 6-cycle ARB processed specimen at 773 K for 1.8 ks induced no recrystallization but only recovery of austenite, resulting in the same transformation texture and variant selection rule with those in the 6-cycle ARB processed specimen. In contrast, annealing treatment of the 6-cycle ARB processed austenite at 873 K for 1.8 ks suppressed the variant selection by changing the austenite structure from elongated ultrafine-grains to

fully-recrystallized and equiaxed fine-grains.

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